TRIS. III. THE DIFFUSE GALACTIC RADIO EMISSION AT δ = +42°
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ABSTRACT

We present values of temperature and spectral index of the Galactic diffuse radiation measured at 600 and 820 MHz along a 24° right ascension circle at declination δ = +42°. They have been obtained from a subset of absolute measurements of the sky temperature made with TRIS, an experiment devoted to the measurement of the CMB temperature at decimetric wavelengths with an angular resolution of about 20°. Our analysis confirms the preexisting picture of the Galactic diffuse emission at decimetric wavelength and improves the accuracy of the measurable quantities. In particular, the signal coming from the halo has a spectral index in the range 2.9 – 3.1 above 600 MHz, depending on the sky position. In the disk, at TRIS angular resolution, the free-free emission accounts for the 11% of the overall signal at 600 MHz and 21% at 1420 MHz. The polarized component of the Galactic emission, evaluated from the survey by Brouw and Spoelstra, affects the observations at TRIS angular resolution by less than 3% at 820 MHz and less than 2% at 600 MHz. Within the uncertainties, our determination of the Galactic spectral index is practically unaffected by the correction for polarization. Since the overall error budget of the sky temperatures measured by TRIS at 600 MHz, that is, 66 (systematic) + 18 (statistical) mK, is definitely smaller than those reported in previous measurements at the same frequency, our data have been used to discuss the zero levels of the sky maps at 150, 408, 820, and 1420 MHz in literature. Concerning the 408 MHz survey, limiting our attention to the patch of sky corresponding to the region observed by TRIS, we suggest a correction of the base level of +3.9 ± 0.6 K.

Subject headings: cosmic microwave background — diffuse radiation

1. INTRODUCTION

Measurements of brightness temperature and frequency spectrum of the Galactic radio emission are of primary importance for astrophysics. There are tight links between the radio signal and the cosmic-ray electrons (CREs) that, moving through the interstellar magnetic field, produce synchrotron radiation. A detailed knowledge of the Galactic radio emission is also important for observational cosmology. The Galactic radio emission is a foreground that hampers the search and detection of spectral distortions, anisotropies, and residual polarization of the cosmic microwave background (CMB). Here we present and discuss results on the diffuse Galactic emission at decimetric wavelengths obtained with TRIS, an experiment dedicated to the search for CMB spectral distortions, which included a subset of observations especially made to extract the Galactic signal. The complete experiment and its cosmological results are presented in Zannoni et al. (2008, hereafter Paper I) and Gervasi et al. (2008b, hereafter Paper II). TRIS is a system of three absolute radiometers operating at nominal frequencies of 600, 820, and 2500 MHz, respectively, installed at Campo Imperatore (Italy, latitude = +42°). To minimize the level of radio interferences at the observing site, the receivers were tuned at 600.5, 817.75, and 2427.75 MHz. The three antennas, wavelength-scaled pyramidal horns with the same beam (HPBW_H × HPBW_E = 23° × 18°) at the three frequencies, were aimed at the zenith with their E-planes tilted 7° westward from the meridian. Along the right ascension, in a direction nearly parallel to the antennas’ H-plane, the size of the beams have been used in two different operation modes: (1) in drift-scan mode to measure profiles of the variations of the sky temperature versus the right ascension α, along a circle of constant declination δ = +42°; and (2) in absolute mode, to get the absolute temperature of the sky at various points along the same circle. This configuration guarantees that the same sky region can be observed with the same beam at different frequencies, so that the comparison of the signals is straightforward. Moreover, every 24 hr a complete profile (drift-scan profile) of the antenna temperature T_a versus α is obtained. After subtraction of the local (ground and atmospheric) contributions, data collected at nighttime at different epochs during a year are combined in a profile of T_{sky}, the sky brightness temperature, covering the full right ascension range at δ = +42° (Paper I). The sky signal is a superposition of isotropic components of extragalactic origin, that is, CMB and unresolved extragalactic radio sources (UERSs; see Gervasi et al. 2008a), and the anisotropic Galactic signal:

\[ T_{sky}(\nu, \alpha, \delta) = T_{Gal}(\nu, \alpha, \delta) + T_{UERS}(\nu) + T_{CMB}(\nu), \]

where \( T_{Gal} \propto \nu^{-\beta_{Gal}} \). The undefined frequency dependence of \( T_{CMB} \) that appears in equation (1) accounts for possible spectral distortions of the CMB. Variations of \( T_{sky} \) versus \( \alpha \) are due only to \( T_{Gal} \). Analyzing these variations by means of the TT-plot technique proposed by Turtle et al. (1962), we obtain \( \beta_{Gal}^{TT} \). Having \( \beta_{Gal}^{TT} \), it is then possible to disentangle the components of \( T_{sky} \) (Paper II) and get absolute values of \( T_{Gal} \). An important remark is that the physical interpretation of the values of \( \beta_{Gal} \) found by means of this technique is not always straightforward. In particular, near the Galactic plane, the spectral index of the diffuse emission found in this way is really produced by a blend of synchrotron and free-free emission. A possible approach followed by some authors (e.g., Platania et al. 1998) to extract the thermal contribution near the Galactic plane, in particular at frequencies higher than 1 GHz, is to use an H II catalog.

The outline of the paper is the following. In § 2 we describe the data set we used in our analysis. Then we show the results obtained using just genuine TRIS data in § 3, while a more general discussion, including also polarization effects, can be found in § 4.
where our data set is fully exploited. The astrophysical issues and possible hints for future experiments are discussed in § 5, followed by a last section summarizing the results (§ 6).

2. THE DATA SET

In this section we describe the starting point of our analysis, that is, the data collected during the TRIS observational campaigns in drift-scan mode and the sky profiles extracted from extended radio surveys at 150, 408, 820, and 1420 MHz.

2.1. TRIS: Drift Scans and Absolute Measurements

From Paper I we take the two absolute profiles of $T_{\text{sky}}$ versus $\alpha$ at $\delta = +42^\circ$ measured at 600 and 820 MHz, respectively. The data collected by TRIS at 2500 MHz cover only small portions of the right ascension circle observed at lower frequencies; moreover, in these portions, variations of $T_{\text{sky}}$ versus $\alpha$, necessary to recognize the Galactic contribution, are of the same order of the accuracy of $T_{\text{sky}}$. They are less accurate than other data in literature at the same frequency (Sironi et al. 1984).

2.2. Sky Profiles from Other Radio Surveys

In order to obtain a more reliable (and more complete) study of the spectral index variation across the sky at $\delta = +42^\circ$, we decided to use also the 408 MHz (Haslam et al. 1982) and 1420 MHz (Reich & Reich 1986) surveys, both of them in the destriped version produced by Platania et al. (2003). We have extracted from their maps a sky profile at the declination observed by TRIS, assuming an elliptical $23^\circ \times 18^\circ$ beam, and taking into account the orientation of the E-plane with respect to the meridian. Since the TT-plot technique is not sensitive to zero-offset uncertainties, we considered the extracted profiles affected just by uncertainty on the temperature scale, whose values at 408 and 1420 MHz are, respectively, 10% and 5%. To have a wider frequency coverage, we used also the 50 MHz resolution map at 150 MHz prepared by Landecker & Wielebinski (1970) using their Southern Sky survey at 150 MHz and the 178 MHz survey by Turtle & Baldwin (1962). In this case, the reported temperature scale uncertainty is 5%.

Since we used single-polarization radiometers, we decided to check the consistency of our results exploiting also the Leiden polarization survey at 610 and 820 MHz (Brouw & Spoelstra 1976). Finally, we compared our absolute sky profile at $\delta = +42^\circ$ with the corresponding one extracted from the Dwingeloo northern sky survey at 820 MHz (Berghuijsen 1972).

2.3. The Unresolved Extragalactic Radio Sources

The contribution of the UERSs to the brightness temperature collected by our antennas can be considered as an isotropic signal scaling with frequency as a power law with spectral index $\gamma_{u,\text{ERS}} \sim -2.70$. A detailed study of this signal, presented in a dedicated paper (Gervasi et al. 2008a and references therein), allowed us to disentangle the components of the celestial signal and, finally, to recover the amplitude of the Galactic radio emission.

3. TRIS

3.1. Methods of Extraction of the Galactic Spectral Index

Two methods can be used to extract the Galactic spectral index:

1. Differential method.—Based on the TT-plot method (Turtle et al. 1962), it can be used when values of $T_{\text{sky}}$ measured at different positions on the sky at two frequencies are available, no matter if the zeros of the scales of temperature at frequencies $\nu_1$ and $\nu_2$ are known. Combining equation (1) written for two frequencies $\nu_1$ and $\nu_2$, we obtain

$$T_{\text{sky}}(\nu_2, \alpha, \delta) = T_{\text{sky}}(\nu_1, \alpha, \delta) \left( \frac{\nu_2}{\nu_1} \right)^{-\beta_{\text{Gal}}(\alpha, \delta; \nu_1, \nu_2)} + T_{\text{ERS}}(\nu_1) \left( \frac{\nu_2}{\nu_1} \right)^{-\gamma_{\text{ERS}}(\nu_2, \nu_1)} - \left( \frac{\nu_2}{\nu_1} \right)^{-\beta_{\text{Gal}}(\alpha, \delta; \nu_1, \nu_2)} + \left[ T_{\text{CMB}}(\nu_2) - T_{\text{CMB}}(\nu_1) \left( \frac{\nu_2}{\nu_1} \right)^{-\beta_{\text{Gal}}(\alpha, \delta; \nu_1, \nu_2)} \right].$$

(2)

In a sky region where $\beta_{\text{Gal}}$ does not depend on position, a plot of $T_{\text{sky}}(\alpha, \delta; \nu_2)$ versus $T_{\text{sky}}(\alpha, \delta; \nu_1)$ is a straight line of slope

$$m = \left( \frac{\nu_2}{\nu_1} \right)^{-\beta_{\text{Gal}}(\alpha_0, \delta_0; \nu_1, \nu_2)},$$

(3)

where $\alpha_0$ and $\delta_0$ are the values of $\alpha$ and $\delta$ at the center of the region used to build the TT-plot. Conversely, if the spectral index is not constant, loops and V-shaped features appear in the TT-plot. The spectral index representative of the uniform region centered on $\alpha_0$ and $\delta_0$ is immediately obtained from $m$. Let us call it the “average” or $\beta_{\text{Gal}}(\alpha_0, \delta_0; \nu_1, \nu_2)$ spectral index. It depends only on variations of $T_{\text{sky}}$ and is independent of the zero level of the scales of temperature used at $\nu_1$ and $\nu_2$.

2. Direct method.—When the absolute values of $T_{\text{Gal}}(\alpha, \delta, \nu)$ at a given position $(\alpha, \delta)$ are known at two frequencies, we can write

$$\beta_{\text{Gal}}(\alpha, \delta; \nu_1, \nu_2) = -\frac{\log[T_{\text{Gal}}(\alpha, \delta, \nu_1)/T_{\text{Gal}}(\alpha, \delta, \nu_2)]}{\log(\nu_1/\nu_2)},$$

(4)

Let us call it the “local” spectral index.

Differential and direct methods, whose advantages and limitations have been described in Lawson et al. (1987), are affected by systematics in completely orthogonal ways. The local spectral index is prone to the effect of wrong zero levels (see eq. [4]), but once we are confident that our absolute measurements are correct for systematics, we can use this technique over the complete range of right ascension, regardless of the nature of the physical properties of the observed regions. Conversely, $\beta_{\text{Gal}}(\alpha_0, \delta_0; \nu_1, \nu_2)$ is not affected by temperature offsets, but it is not well determined over all the sky because the TT-plot is effective whenever (1) $\beta_{\text{Gal}}$ is only weakly dependent on celestial coordinates thanks to the homogeneity of the observed region and (2) the intensity of the signal varies appreciably through space. Since these conditions are not met everywhere, the TT-plot method cannot be used to get a well-defined value of the spectral index at every point in the sky.

In the case of TRIS, in the sky regions where the TT-plot technique provides reliable results, we show that $\beta_{\text{Gal}}$, which intrinsically represents a spatially averaged value of the spectral index, coincides with the local value of $\beta_{\text{Gal}}$ (eq. [4]). This is an important cross-check since, if the results are consistent within the uncertainties, then we can exclude undetected systematics affecting the zero levels of our absolute temperature scans, as we show in § 3.3. If this is true, we may overcome the limitations of the TT-plot and assign a value of the local spectral index point by point in the sky.

3.2. TRIS Results

3.2.1. Spectral Index from TT-Plots

We apply the differential method to the pair of drift scans at 600 and 820 MHz measured by TRIS. As expected (see, e.g.,
Sironi 1974), the pattern produced by the complete set of $T_{sk}(\alpha)$ in the range $0^h \leq \alpha \leq 24^h$ is far from a straight line because $\beta_{Gal}$ varies with $\alpha$. There are, however, two right ascension intervals along the circle at declination $+42^\circ$ where straight lines are clearly defined and $\beta_{TT}^{Gal}$ can be obtained (see Fig. 1). The first region covers the right ascension interval $09^h \leq \alpha_0 \leq 11^h$: it is characterized by a minimum of the sky brightness temperature and signals come from the Galactic halo. The second region is at $19^h \leq \alpha_0 \leq 21^h$. Here the sky temperature reaches a maximum and the signal comes essentially from the Galactic disk.

In Table 1 we show the values of $\beta_{TT}^{Gal}$ measured in these regions and the width $\Delta \alpha$ of the right ascension interval used to build the TT-plot. Lower limits on $\Delta \alpha$ are set by the beam size of TRIS antennas and by the statistical significance we want to assign to the parameters extracted from the linear fit (for two parameters, slope and intercept, the degrees of freedom (dof) are $(2\Delta \alpha/\text{FWHM}) - 2$). An upper limit on $\Delta \alpha$ is set by the appearance in the plot of deviations from a straight line, due to the fact that we are considering a region wider than the homogeneity scale of the interstellar medium. We accepted fits with a $\chi^2$ probability $Q$ (as defined in Press et al. 1992) greater than 0.1. The effective values of $Q$ and $\chi^2$/dof are also shown in Table 1, together with $\beta_{TT, \text{robust}}^{Gal}$, an estimate of the Galactic spectral index obtained using a robust straight line fitting function (Hoaglin et al. 1983). The agreement within the uncertainties of $\beta_{TT}^{Gal}$ and $\beta_{TT, \text{robust}}^{Gal}$ shows that the selection criteria of the areas we use are properly chosen.

### 3.2.2. Galactic Temperature and the Local Spectral Index

The above values of $\beta_{TT}^{Gal}$ cover only part of the full right ascension circle at $\delta = +42^\circ$ explored by TRIS. However, combined with absolute measurement of $T_{sk}$ made by TRIS, they are sufficient to disentangle the components of $T_{sk}$ and get absolute values of $T_{Gal}$ at 600 and 820 MHz at every point along the circle at $\delta = +42^\circ$. This is done in Paper II. After corrections for polarization effects (see § 4.1), the resulting values of $T_{Gal}$ are used to get by equation (4) the local spectral index between 600 and 820 MHz.

### Table 1

**TT-Plots: Spectral Index between TRIS Data at 600 and 820 MHz**

<table>
<thead>
<tr>
<th>$\alpha_0$</th>
<th>$\beta_{TT}^{Gal}$</th>
<th>$\chi^2$/dof</th>
<th>$Q$</th>
<th>$\beta_{TT, \text{robust}}^{Gal}$</th>
<th>$\Delta \alpha$</th>
</tr>
</thead>
<tbody>
<tr>
<td>09 00 00..............</td>
<td>3.0 ± 0.1</td>
<td>0.48</td>
<td>0.85</td>
<td>2.97 ± 0.01</td>
<td>105</td>
</tr>
<tr>
<td>10 00 00..............</td>
<td>3.1 ± 0.1</td>
<td>0.42</td>
<td>0.89</td>
<td>3.06 ± 0.02</td>
<td>105</td>
</tr>
<tr>
<td>11 00 00..............</td>
<td>3.1 ± 0.2</td>
<td>0.50</td>
<td>0.84</td>
<td>3.13 ± 0.04</td>
<td>105</td>
</tr>
<tr>
<td>19 00 00..............</td>
<td>2.7 ± 0.1</td>
<td>1.17</td>
<td>0.32</td>
<td>2.79 ± 0.02</td>
<td>75</td>
</tr>
<tr>
<td>20 00 00..............</td>
<td>2.73 ± 0.09</td>
<td>1.15</td>
<td>0.33</td>
<td>2.75 ± 0.02</td>
<td>105</td>
</tr>
<tr>
<td>20 24 00..............</td>
<td>2.8 ± 0.1</td>
<td>0.95</td>
<td>0.46</td>
<td>2.75 ± 0.02</td>
<td>105</td>
</tr>
<tr>
<td>21 00 00..............</td>
<td>2.7 ± 0.1</td>
<td>0.98</td>
<td>0.44</td>
<td>2.69 ± 0.02</td>
<td>90</td>
</tr>
</tbody>
</table>

**Note.** Units of right ascension are hours, minutes, and seconds.
plotted here are reported in Table 2 with the corresponding uncertainties. Spoestra (1976) and Spoestra (1984) is also taken into account. Some of the data corrected for polarization and values of $\alpha$.

spectral index coincide within the uncertainties (see Table 3). As expected, the local Galactic spectral index calculated including or not including the polarization effects.

820 MHz. In Table 2 and Figures 2 and 3 we show values of $T_{\text{Gal}}$ corrected for polarization and values of $\beta_{\text{loc, pol}}$ and $\beta_{\text{Gal, pol}}$, respectively, the local spectral index corrected and not corrected for polarization effects. The values of $T_{\text{Gal}}$ corrected for polarization are used to get, by the TT-plot method, values of $\beta_{\text{Gal, pol}}$. The values of $\beta_{\text{Gal, pol}}$ corrected for polarization are shown in Table 3. As expected, the smoothing effects of the large beam of the TRIS antennas make statistically negligible the differences between the values of the

\begin{table}[h]
\centering
\begin{tabular}{|c|c|c|c|}
\hline
$\alpha$ & $T_{\text{Gal, 600}} + \Delta T_{\text{600}}^{\text{pol}}$ (K) & $T_{\text{Gal, 820}} + \Delta T_{\text{820}}^{\text{pol}}$ (K) & $\beta_{\text{800-820}}$ \\
\hline
00 00 00 & 11.38 ± 0.07 & 4.61 ± 0.03 & 2.92 ± 0.03 & 2.93 ± 0.03 \\
01 00 00 & 11.48 ± 0.07 & 4.77 ± 0.03 & 2.85 ± 0.03 & 2.87 ± 0.03 \\
02 00 00 & 12.32 ± 0.08 & 5.17 ± 0.04 & 2.80 ± 0.03 & 2.80 ± 0.03 \\
03 00 00 & 13.08 ± 0.08 & 5.54 ± 0.04 & 2.79 ± 0.03 & 2.79 ± 0.02 \\
04 00 00 & 13.60 ± 0.07 & 5.63 ± 0.04 & 2.85 ± 0.03 & 2.89 ± 0.02 \\
05 00 00 & 13.47 ± 0.08 & 5.44 ± 0.04 & 2.93 ± 0.03 & 3.00 ± 0.02 \\
06 00 00 & 11.87 ± 0.08 & 4.73 ± 0.04 & 2.99 ± 0.04 & 3.04 ± 0.03 \\
07 00 00 & 9.85 ± 0.08 & 3.81 ± 0.04 & 3.07 ± 0.04 & 3.10 ± 0.03 \\
08 00 00 & 7.95 ± 0.07 & 3.03 ± 0.03 & 3.12 ± 0.05 & 3.14 ± 0.04 \\
09 00 00 & 6.37 ± 0.07 & 2.40 ± 0.03 & 3.10 ± 0.05 & 3.11 ± 0.05 \\
10 00 00 & 5.72 ± 0.07 & 2.21 ± 0.03 & 3.08 ± 0.06 & 3.07 ± 0.06 \\
11 00 00 & 5.85 ± 0.07 & 2.21 ± 0.03 & 3.16 ± 0.06 & 3.15 ± 0.06 \\
12 00 00 & 6.39 ± 0.07 & 2.34 ± 0.03 & 3.22 ± 0.06 & 3.21 ± 0.05 \\
13 00 00 & 6.51 ± 0.07 & 2.48 ± 0.03 & 3.12 ± 0.05 & 3.12 ± 0.05 \\
14 00 00 & 6.97 ± 0.07 & 2.73 ± 0.03 & 3.04 ± 0.05 & 3.06 ± 0.05 \\
15 00 00 & 7.63 ± 0.07 & 3.01 ± 0.03 & 3.01 ± 0.04 & 3.03 ± 0.04 \\
16 00 00 & 8.37 ± 0.07 & 3.29 ± 0.03 & 3.02 ± 0.04 & 3.02 ± 0.04 \\
17 00 00 & 9.27 ± 0.07 & 3.79 ± 0.03 & 2.86 ± 0.04 & 2.88 ± 0.03 \\
18 00 00 & 10.98 ± 0.07 & 4.85 ± 0.03 & 2.66 ± 0.03 & 2.67 ± 0.03 \\
19 00 00 & 15.44 ± 0.08 & 6.54 ± 0.03 & 2.77 ± 0.02 & 2.78 ± 0.02 \\
20 00 00 & 23.26 ± 0.08 & 9.72 ± 0.03 & 2.82 ± 0.01 & 2.82 ± 0.01 \\
21 00 00 & 24.44 ± 0.07 & 10.38 ± 0.03 & 2.78 ± 0.01 & 2.78 ± 0.01 \\
22 00 00 & 21.87 ± 0.07 & 9.36 ± 0.03 & 2.75 ± 0.01 & 2.75 ± 0.01 \\
23 00 00 & 15.56 ± 0.07 & 6.65 ± 0.03 & 2.76 ± 0.02 & 2.76 ± 0.02 \\
24 00 00 & 12.44 ± 0.07 & 5.05 ± 0.03 & 2.90 ± 0.03 & 2.90 ± 0.03 \\
\hline
\end{tabular}
\caption{The Brightness Temperature of the Galaxy and the Local Spectral Index between 600 and 820 MHz after Correction for Polarization.}
\end{table}

Notes.—The local Galactic spectral index evaluated from TRIS data not corrected for polarization (see Table 2) is reported in the last column. Units of right ascension are hours, minutes, and seconds.

Fig. 2.—Brightness temperature of the Galaxy at 600 (upper line) and 820 MHz (lower line) after the separation of the celestial signal into primordial (CMB), extragalactic, and Galactic contributions. The correction for polarization based on Brown & Spoestra (1976) and Spoestra (1984) is also taken into account. Some of the data plotted here are reported in Table 2 with the corresponding uncertainties.

Fig. 3.—Bottom: Local spectral index $\beta$ at $\delta = +42^\circ$ shown in detail along the full right ascension range. We show also the values of $\beta_{\text{Gal}}$ in the region where it has been accurately determined (open diamonds). In the same regions we plot the values of $\beta_{\text{Gal}}$ (filled circles) accompanied by the corresponding uncertainties. Top and middle: Galactic latitude and longitude of the points along the circle at constant declination where TRIS observations were made.
Tables 1 and 2 and bottom panel of Fig. 3). It means that the evaluations of the zero levels of the scales of temperature made in Paper I are correct and the systematic uncertainties $|\Delta T_{\text{sys600}}| \leq 66$ mK and $|\Delta T_{\text{sys820}}| \leq 659$ mK we associated with the absolute values of $T_{\text{sky}}$ in Paper I are safe. We cannot, however, exclude that these bars are overestimated. They were in fact set by laboratory measurements of the losses of all the front-end components of the TRIS radiometers.

These uncertainties can be further constrained if we exclude unphysical situations they may imply. We can write

$$
\beta_{\text{Gal}}^\beta(\alpha; \Delta T_{\text{sys600}}, \Delta T_{\text{sys820}}) = \frac{\log [T_{\text{Gal}}(\nu_1; \alpha) + \Delta T_{\text{sys600}}]/[T_{\text{Gal}}(\nu_2; \alpha) + \Delta T_{\text{sys820}}]}{\log(\nu_2/\nu_1)}
$$

and

$$
d(\alpha; \Delta T_{\text{sys600}}, \Delta T_{\text{sys820}}) = \frac{|\beta_{\text{Gal}}^\beta(\alpha; \Delta T_{\text{sys600}}, \Delta T_{\text{sys820}}) - \beta_{\text{Gal}}^{TT}(\alpha)|}{\sigma_{\beta_{\text{Gal}}^\beta(\alpha)} + \sigma_{\beta_{\text{Gal}}^{TT}(\alpha)}}.
$$

where $d$ is the difference between the local and the average spectral index, in standard deviation units. We then let the two $\Delta T_{\text{sys}}$ vary in such a way that $d \leq 2$, while the spectral index stays inside an a priori defined range of physical values. This is done using the TRIS data collected between $\alpha = 9^h$ and $11^h$, where $T_{\text{Gal}}$ is dominated by the synchrotron emission of the cosmic-ray electrons and $\beta_{\text{Gal}} \approx \beta_{\text{syn}}$ (see § 4.3).

Measurements of the spectrum of the CREs (see, e.g., Agrinier et al. 1964; Hartmann et al. 1977; Nishimura et al. 1990; Aguilar et al. 2002; Grimani et al. 2002) and the diffusion process of the electrons in the Galaxy (e.g., Longair 1994 and references therein) allow us to assume that, between 600 and 820 MHz, in the direction of the Galactic halo, a safe a priori condition is $2.6 \leq \beta_{\text{syn}} \leq 3.6$. This choice constrains $\Delta T_{\text{sys820}}$ inside the range (−300 mK, +430 mK). No constraints are obtained at 600 MHz, nor using TRIS data from other regions of sky, i.e., the Galactic disk, where the presence of the thermal bremsstrahlung makes a priori choices less reliable.

4. GENERAL ANALYSIS

4.1. Correction for Polarization Effects

In order to evaluate polarization effects on our analysis (particularly on the determination of the spectral index), we corrected TRIS data with a contribution calculated from the surveys by Brouw and Spoelstra$^3$ at 610 and 820 MHz (see Brouw & Spoelstra 1976; discussion in Spoelstra 1984) convolved with the TRIS beam, knowing the orientation of the polarization plane of TRIS antennas point by point in the sky. In this way we have been able to project the polarized signal into copolar ($T_{\text{copol}}$) and crosspolar ($T_{\text{pol}}$) components at the two frequencies (see Fig. 4). Then we have rescaled the 610 MHz sky profile to 600 MHz by means of

![Fig. 4.—Top: Copolar and cross-polar temperature (K) vs. right ascension extracted from the Brouw and Spoelstra 610 MHz map (Brouw & Spoelstra 1976) with respect to the TRIS antennas’ E-plane and diluted on the 23’ × 18’ beam. Bottom: Same as the top panel, but at 820 MHz.](image-url)
the spectral index derived from TRIS data alone. Finally, we obtained the antenna temperature of the sky corrected for polarization:

$$T_{\text{sky}}(\alpha; \nu) = T_{\text{TRIS}}(\alpha; \nu) - T_{\text{copol}}(\alpha; \nu) + \sqrt{T_{\text{copol}}^2(\alpha; \nu) + T_{\text{qpol}}^2(\alpha; \nu)}.$$  

These corrected sky profiles can be used to evaluate the spectral index by means of TT-plots (eq. [2]), or using equation (4), since we have absolute temperature profiles. The results, concerning the local Galactic spectral index, are presented in Table 2, together with the corrected temperatures, and shown in Figure 5. A comparison between the results reported in Tables 1 and 3 (obtained after polarization correction) gives an estimate of the effect of polarization on the spectral index ($\Delta \beta_{\text{Gal}}$) for an experiment with FWHM $\sim 20^\circ$. $\Delta \beta_{\text{Gal}}$ is zero on the Galactic disk toward the center direction, and $\Delta \beta_{\text{Gal}} \approx -0.1$ toward the halo, where, anyway, the effect is comparable with the uncertainties.

TRIS data, after correction for polarization, have been used also in combination with sky profiles at $\delta = +42^\circ$ extracted from surveys at 150, 408, and 1420 MHz, always using the TT-plot technique, described in § 3.1. The criteria used to single out acceptable values of the fitting parameters are the same as described in § 3.2.1. The results are shown in Tables 4–7. A summary of the results obtained in four distinct sky positions, namely, the Galactic halo ($\alpha = 09^h00^m$, $10^h00^m$, and $11^h00^m$ at $\delta = +42^\circ$) and the Galactic disk ($\alpha = 20^h24^m$, at the same declination), is shown in Table 8.

4.2. A New Assessment of the Zero Level of Continuum Surveys

The temperatures measured by TRIS at 600 MHz have accuracies of 66 (systematics) + 18 (statistics) mK on $T_{\text{sky}}$ and $\sim 70$ mK on $T_{\text{Gal}}$ (Papers I and II). They are definitely more accurate than previous measurements in literature at the same frequency (Sironi et al. 1990 and references therein). This accuracy has been exploited to revise and sometimes improve the accuracy of the zero level of the maps of the radio continuum at 150, 408, 610, 820, and 1420 MHz in literature. This is done comparing profiles extracted from these maps with profiles obtained at the same frequency by extrapolation of the astrophysical signals (Galaxy, UERSs, and CMB) contributing to the $T_{\text{sky}}$ measured by TRIS at 600 MHz.

The comparison is made at $(\alpha_{\text{m}} = 10^h00^m, \delta_{\text{m}} = +42^\circ)$, where $T_{\text{sky}}(600)$ reaches a minimum, $\beta_{\text{Gal}}^T$ and $\beta_{\text{Gal}}^Q$ are both well defined, and $T_{\text{sky}}$ has a weak dependence on the celestial coordinates. Here minor antenna pointing errors, projection effects, and discrepancies between the TRIS beam and the synthesized beam assumed in making map convolutions have a negligible impact on the determination of the antenna temperature at TRIS resolution.

The starting point of this analysis is the first line in Table 9, where we recall the amplitude of the three signals contributing to the sky temperature measured by TRIS at 600 MHz at $(\alpha_{\text{m}}, \delta_{\text{m}})$. Then, knowing the spectral index determined by means of TT-plots, we evaluated the Galactic contribution at the frequencies of the different surveys, from 150 to 1420 MHz. These values are reported in the second column of Table 9, where the quoted uncertainties are obtained propagating both the uncertainty on the spectral index obtained between 600 MHz and the considered frequency (see Table 8 for a summary) and the uncertainty on the amplitude of the Galactic signal at 600 MHz. The third column in Table 9 recalls the estimates of the extragalactic contribution calculated by Gervasi et al. (2008a). The fourth column is the brightness temperature of the CMB measured at 600 MHz, accompanied by its overall uncertainty. All three contributions are then combined in the fifth column, $T_{\text{eval}}(\alpha_{\text{m}}, \delta_{\text{m}})$, which, in turn, is compared with the temperature of the sky profiles extracted from the surveys, reported in the sixth column, with associated zero-level systematics quoted in literature. The difference between the two, $T_{\text{eval}}(\alpha_{\text{m}}, \delta_{\text{m}}) - T_{\text{map}}(\alpha_{\text{m}}, \delta_{\text{m}})$, reported in the last column, gives the correction we suggest to apply to the zero levels of the maps used throughout this work.

At 150 MHz the zero-level adjustment is large, but comparable to the accuracy of the old zero level. At 408 and 820 MHz adjustments accuracies are significant and cannot be ignored. At 1420 MHz no base-level correction is necessary, but the accuracy is improved by a factor of 3.

### TABLE 4

**TT-Plots: Spectral Index between 408 and 600 MHz**

<table>
<thead>
<tr>
<th>$\alpha_0$</th>
<th>$\beta_{\text{Gal}}^T$</th>
<th>$\chi^2_{\text{dof}}$</th>
<th>$Q$</th>
<th>$\beta_{\text{Gal}}^Q$</th>
<th>$\Delta \alpha$ (deg)</th>
</tr>
</thead>
<tbody>
<tr>
<td>09 00 00...</td>
<td>2.58 ± 0.09</td>
<td>0.68</td>
<td>0.69</td>
<td>2.66 ± 0.01</td>
<td>105</td>
</tr>
<tr>
<td>10 00 00...</td>
<td>2.5 ± 0.1</td>
<td>0.55</td>
<td>0.80</td>
<td>2.51 ± 0.02</td>
<td>105</td>
</tr>
<tr>
<td>11 00 00...</td>
<td>2.3 ± 0.2</td>
<td>0.46</td>
<td>0.87</td>
<td>2.35 ± 0.04</td>
<td>105</td>
</tr>
<tr>
<td>19 00 00...</td>
<td>2.80 ± 0.08</td>
<td>0.76</td>
<td>0.57</td>
<td>2.77 ± 0.02</td>
<td>75</td>
</tr>
<tr>
<td>20 00 00...</td>
<td>2.83 ± 0.08</td>
<td>0.90</td>
<td>0.51</td>
<td>2.76 ± 0.02</td>
<td>105</td>
</tr>
<tr>
<td>20 24 00...</td>
<td>2.82 ± 0.09</td>
<td>0.95</td>
<td>0.47</td>
<td>2.75 ± 0.02</td>
<td>105</td>
</tr>
<tr>
<td>21 00 00...</td>
<td>2.7 ± 0.1</td>
<td>0.80</td>
<td>0.56</td>
<td>2.67 ± 0.02</td>
<td>90</td>
</tr>
</tbody>
</table>

**Note.** — Units of right ascension are hours, minutes, and seconds.
TABLE 5
TT Plots: Spectral Index between 408 and 820 MHz

<table>
<thead>
<tr>
<th>α0</th>
<th>βTGal</th>
<th>χ²/dof</th>
<th>Q</th>
<th>βTTrobest</th>
<th>Δαα (deg)</th>
</tr>
</thead>
<tbody>
<tr>
<td>09 00 00</td>
<td>2.74 ± 0.08</td>
<td>0.38</td>
<td>0.92</td>
<td>2.75 ± 0.01</td>
<td>105</td>
</tr>
<tr>
<td>10 00 00</td>
<td>2.7 ± 0.1</td>
<td>0.41</td>
<td>0.90</td>
<td>2.72 ± 0.01</td>
<td>105</td>
</tr>
<tr>
<td>11 00 00</td>
<td>2.7 ± 0.2</td>
<td>0.43</td>
<td>0.88</td>
<td>2.65 ± 0.03</td>
<td>105</td>
</tr>
<tr>
<td>19 00 00</td>
<td>2.79 ± 0.09</td>
<td>0.75</td>
<td>0.57</td>
<td>2.78 ± 0.02</td>
<td>75</td>
</tr>
<tr>
<td>20 00 00</td>
<td>2.81 ± 0.09</td>
<td>0.68</td>
<td>0.69</td>
<td>2.76 ± 0.01</td>
<td>105</td>
</tr>
<tr>
<td>20 24 00</td>
<td>2.8 ± 0.1</td>
<td>0.65</td>
<td>0.72</td>
<td>2.75 ± 0.02</td>
<td>105</td>
</tr>
<tr>
<td>21 00 00</td>
<td>2.8 ± 0.1</td>
<td>0.70</td>
<td>0.64</td>
<td>2.69 ± 0.02</td>
<td>90</td>
</tr>
</tbody>
</table>

Note.—Units of right ascension are hours, minutes, and seconds.

TABLE 6
TT-Plots: Spectral Index between 600 and 1420 MHz

<table>
<thead>
<tr>
<th>α0</th>
<th>βTGal</th>
<th>χ²/dof</th>
<th>Q</th>
<th>βTTrobest</th>
<th>Δαα (deg)</th>
</tr>
</thead>
<tbody>
<tr>
<td>09 00 00</td>
<td>2.84 ± 0.07</td>
<td>1.56</td>
<td>0.14</td>
<td>2.85 ± 0.01</td>
<td>105</td>
</tr>
<tr>
<td>10 00 00</td>
<td>2.8 ± 0.1</td>
<td>1.68</td>
<td>0.11</td>
<td>2.81 ± 0.03</td>
<td>105</td>
</tr>
<tr>
<td>11 00 00</td>
<td>3.1 ± 0.3</td>
<td>1.67</td>
<td>0.11</td>
<td>2.94 ± 0.07</td>
<td>105</td>
</tr>
<tr>
<td>19 00 00</td>
<td>2.57 ± 0.07</td>
<td>0.31</td>
<td>0.89</td>
<td>2.60 ± 0.01</td>
<td>75</td>
</tr>
<tr>
<td>20 00 00</td>
<td>2.54 ± 0.08</td>
<td>0.72</td>
<td>0.63</td>
<td>2.59 ± 0.02</td>
<td>105</td>
</tr>
<tr>
<td>20 24 00</td>
<td>2.55 ± 0.08</td>
<td>0.70</td>
<td>0.68</td>
<td>2.60 ± 0.01</td>
<td>105</td>
</tr>
<tr>
<td>21 00 00</td>
<td>2.6 ± 0.1</td>
<td>0.71</td>
<td>0.64</td>
<td>2.64 ± 0.02</td>
<td>90</td>
</tr>
</tbody>
</table>

Note.—Units of right ascension are hours, minutes, and seconds.

TABLE 7
TT-Plots: Spectral Index between 820 and 1420 MHz

<table>
<thead>
<tr>
<th>α0</th>
<th>βTGal</th>
<th>χ²/dof</th>
<th>Q</th>
<th>βTTrobest</th>
<th>Δαα (deg)</th>
</tr>
</thead>
<tbody>
<tr>
<td>09 00 00</td>
<td>2.8 ± 0.1</td>
<td>0.93</td>
<td>0.48</td>
<td>2.84 ± 0.02</td>
<td>105</td>
</tr>
<tr>
<td>10 00 00</td>
<td>2.7 ± 0.2</td>
<td>1.69</td>
<td>0.11</td>
<td>2.71 ± 0.04</td>
<td>105</td>
</tr>
<tr>
<td>11 00 00</td>
<td>3.3 ± 0.6</td>
<td>1.69</td>
<td>0.18</td>
<td>2.92 ± 0.12</td>
<td>105</td>
</tr>
<tr>
<td>19 00 00</td>
<td>2.50 ± 0.10</td>
<td>1.10</td>
<td>0.36</td>
<td>2.46 ± 0.02</td>
<td>75</td>
</tr>
<tr>
<td>20 00 00</td>
<td>2.5 ± 0.1</td>
<td>1.08</td>
<td>0.37</td>
<td>2.50 ± 0.02</td>
<td>105</td>
</tr>
<tr>
<td>20 24 00</td>
<td>2.4 ± 0.1</td>
<td>1.18</td>
<td>0.31</td>
<td>2.52 ± 0.02</td>
<td>105</td>
</tr>
<tr>
<td>21 00 00</td>
<td>2.6 ± 0.2</td>
<td>1.30</td>
<td>0.25</td>
<td>2.60 ± 0.03</td>
<td>90</td>
</tr>
</tbody>
</table>

Note.—Units of right ascension are hours, minutes, and seconds.

TABLE 8
TT-Plots: Summary

<table>
<thead>
<tr>
<th>(ν1, ν2) (MHz)</th>
<th>α = 90°h</th>
<th>α = 10°h</th>
<th>α = 11°h</th>
<th>α = 20°24m</th>
</tr>
</thead>
<tbody>
<tr>
<td>150–408</td>
<td>2.1 ± 0.3</td>
<td>2.2 ± 0.3</td>
<td>2.2 ± 0.3</td>
<td>...</td>
</tr>
<tr>
<td>150–600</td>
<td>2.2 ± 0.2</td>
<td>2.3 ± 0.2</td>
<td>2.4 ± 0.2</td>
<td>...</td>
</tr>
<tr>
<td>150–820</td>
<td>2.4 ± 0.2</td>
<td>2.5 ± 0.2</td>
<td>2.5 ± 0.2</td>
<td>...</td>
</tr>
<tr>
<td>408–600</td>
<td>2.6 ± 0.1</td>
<td>2.5 ± 0.1</td>
<td>2.3 ± 0.2</td>
<td>2.82 ± 0.09</td>
</tr>
<tr>
<td>408–820</td>
<td>2.74 ± 0.08</td>
<td>2.7 ± 0.1</td>
<td>2.7 ± 0.2</td>
<td>2.8 ± 0.1</td>
</tr>
<tr>
<td>600–820</td>
<td>2.91 ± 0.08</td>
<td>3.0 ± 0.1</td>
<td>3.0 ± 0.2</td>
<td>2.8 ± 0.1</td>
</tr>
<tr>
<td>600–1420</td>
<td>2.73 ± 0.07</td>
<td>2.6 ± 0.1</td>
<td>2.4 ± 0.3</td>
<td>2.63 ± 0.07</td>
</tr>
<tr>
<td>600–1420</td>
<td>2.84 ± 0.07</td>
<td>2.8 ± 0.1</td>
<td>3.1 ± 0.3</td>
<td>2.55 ± 0.08</td>
</tr>
<tr>
<td>820–1420</td>
<td>2.8 ± 0.1</td>
<td>2.7 ± 0.2</td>
<td>3.3 ± 0.6</td>
<td>2.4 ± 0.1</td>
</tr>
</tbody>
</table>

Notes.—The Galactic spectral index toward the Galactic halo and at the peak of the Galactic emission at δ = +42°. Here we show the frequencies (ν1 and ν2, in MHz) used to build the TT-plots. Also the Galactic coordinates (l, b) are reported.

2 In this case TRIS data corrected for polarization are used.
4.3. Galactic Spectral Index

In spite of the limited sky coverage of TRIS and the coarse angular resolution of its antennas, the local spectral index and its variations can be tracked along the complete right ascension circle at δ = +42°. It brings information about different Galactic regions going from the halo to the disk. To point out this fact, the values of the local spectral index $\beta_{\text{Gal}} = (a + 3)/2$, where $a$ is the spectral index of the energy spectrum $N(E)dE$ of the CREs responsible for the synchrotron emission. The increase of $\beta_{\text{syn}}$ with $\nu$ is probably a consequence of a knee, at $E_k \sim 1$ GeV, in the CRE energy spectrum: with $a = a_1$ at $E < E_k$ and $a = a_2$ at $E > E_k$. Moreover, extended structures coming out from the disk, such as the Galactic loop III (Berkhuijsen 1971), visible on the all-sky maps, play an important role in the determination of the radio continuum spectral index (Lawson et al. 1987).

4.3.1. The Galactic Halo

From TT-plots centered in regions belonging to the Galactic halo, where the synchrotron is the dominant radiative process, we found that between 150 and 600 MHz, as a consequence of a knee in the energy distribution of CREs, the brightness temperature spectrum index, even if in some cases it is poorly determined, changes from 2.3–2.5 to 2.8–3.0, as we can see in Table 8 and Figure 6. This behavior, observed in the past (e.g., Sironi 1974; Webster 1974), a steepening of the spectrum is observed when the line of sight moves from low to high Galactic latitudes. Dependence on Galactic longitude, which partially masks the latitude dependence, is also visible. This is not surprising because along the circle at $\delta = +42^\circ$ the Galactic disk is crossed twice, in regions where the relative weights of thermal and nonthermal emission are different. Moreover, extended structures coming out from the disk, such as the Galactic loop III (Berkhuijsen 1971), visible on the all-sky maps, play an important role in the determination of the radio continuum spectral index (Lawson et al. 1987).

4.3.2. The Galactic Disk

Moving toward the Galactic disk (see last column in Table 8), the TT-plots between one of the low-frequency sky profiles (408, 600, and 820 MHz) and the 1420 MHz profile show that the radio spectrum flattens from $\sim 2.8$ to $\sim 2.5$, probably because the weight of H II regions, especially at 1420 MHz, is no longer negligible. In this case $\beta$ has to be interpreted as an effective spectral index ($\beta_{\text{eff}}$), which is properly the result of a blend of thermal (free-free) and synchrotron emission. If we have the Galactic temperature at two frequencies $\nu$ and $\nu_0$, then

$$T_\text{Gal}(\nu) = T_\text{syn}(\nu/\nu_0)^{-\beta_{\text{syn}}} + T_\text{ff}(\nu/\nu_0)^{-2.1},$$

while $T_\text{Gal}(\nu)/T_\text{Gal}(\nu_0) = (\nu/\nu_0)^{-\beta_{\text{eff}}}$. Defining $w = T_\text{ff}/T_{\text{syn}}$, the ratio of the free-free and synchrotron contributions at $\nu_0$, we obtain

$$\beta_{\text{eff}} = \log\left\{\left[(\nu/\nu_0)^{-\beta_{\text{syn}}} + w(\nu/\nu_0)^{-2.1}\right]/(1 + w)\right\},$$

where $\beta_{\text{eff}}$ is the well-known critical frequency that links the frequency of synchrotron emission, the energy $E$ of the radiating electron, and the component $B_\perp$ of the magnetic field $B$ orthogonal to the line of sight (e.g., Ginzburg & Syrovatskii 1965).

In Figure 8 we show the contour lines of $\nu_{\text{ex}}$ for the $(E_k, B_\perp)$-plane for $a_1 = 1.7$ (consistent with $\beta_{\text{syn}} \simeq 2.3$, and contained in the range 1.6–1.8 suggested by Strong et al. 2000) and for two values of $a_2$, 2.6 and 3.0, corresponding, respectively, to $\beta_{\text{syn}1} = 2.8$ and $\beta_{\text{syn}2} = 3.0$, the allowed interval of values for $\nu > 600$ MHz according to our analysis. Steeper spectra, reaching also $\beta_{\text{syn}} \simeq 3.3$, can be produced in a scenario in which magnetic inhomogeneities are considered (Cavallo & Sironi 1977), or in the presence of a further steepening of the CRE energy spectrum. In the latter case, the effect on the radio spectrum should be relevant especially at tens of GHz, since $a = 3.6 \pm 0.2$ is found for energies $E \gtrsim 6$ GeV (Boezio et al. 2000).

From the results obtained in the present work, based only on data coming from radio astronomy, we can state that toward the Galactic halo $\nu_{\text{ex}} < 600$ MHz, as we can see in Figures 6 and 7 and Table 8. If we take into account also the spectral index map presented in Roger et al. (1999), where no synchrotron knee is detected between 22 and 408 MHz in the region observed by TRIS, a tighter bound is $408$ MHz $< \nu_{\text{ex}} < 600$ MHz. This constraint on $\nu_{\text{ex}}$ singles out a region of allowed values for $E_k$ and $B_\perp$ (see Fig. 8), but the degeneracy cannot be broken without a further relationship between the knee energy and the Galactic magnetic field provided by the modeling of CRE’s diffusion-loss process with additional data sets (see, e.g., Strong et al. 2000).

### Table 9

<table>
<thead>
<tr>
<th>$\nu$ (MHz)</th>
<th>$T_{\lambda\text{Gal}}(\nu_0)$ (K)</th>
<th>$T_{\Upsilon\text{ERS}}$ (K)</th>
<th>$T_{\lambda\text{MB}}$ (K)</th>
<th>$T_{\text{syn}}(\nu_0)$ (K)</th>
<th>$T_{\text{map}}(\nu_0)$ (K)</th>
<th>$\Delta T$ (K)</th>
</tr>
</thead>
<tbody>
<tr>
<td>TRIS 600</td>
<td>5.63 ± 0.07</td>
<td>0.94 ± 0.03</td>
<td>2.82 ± 0.13</td>
<td>...</td>
<td>...</td>
<td>...</td>
</tr>
<tr>
<td>150°</td>
<td>139 ± 39</td>
<td>39 ± 2</td>
<td>2.82 ± 0.13</td>
<td>180 ± 39</td>
<td>123 ± 40</td>
<td>58 ± 39</td>
</tr>
<tr>
<td>408°</td>
<td>15.0 ± 0.6</td>
<td>2.65 ± 0.09</td>
<td>2.82 ± 0.13</td>
<td>20.5 ± 0.6</td>
<td>16.6 ± 3</td>
<td>3.9 ± 0.6</td>
</tr>
<tr>
<td>820°</td>
<td>2.24 ± 0.07</td>
<td>0.41 ± 0.01</td>
<td>2.82 ± 0.13</td>
<td>5.47 ± 0.15</td>
<td>5.75 ± 0.6</td>
<td>-0.27 ± 0.15</td>
</tr>
<tr>
<td>1420°</td>
<td>0.51 ± 0.04</td>
<td>0.094 ± 0.004</td>
<td>2.82 ± 0.13</td>
<td>3.43 ± 0.14</td>
<td>3.31 ± 0.5</td>
<td>+0.12 ± 0.14</td>
</tr>
</tbody>
</table>

* Haslam et al. (1982).
* Berkhuizen (1972).
* Reich & Reich (1986).
which tells us that $\beta_{\text{eff}} < \beta_{\text{syn}}$, since $w$ is always positive and $\beta_{\text{syn}} > 2.1$.

After the adjustment of base levels described in § 4.2, we used the temperatures in correspondence of the peak of the Galactic signal at 408, 600.5 (TRIS), 817.5 (TRIS), 820, and 1420 MHz to fit the amplitudes of the Galactic components, $T_{\text{syn}}$ and $T_{\text{Gal}}$, and the value of $\beta_{\text{syn}}$. We also imposed that the condition $T_{\text{Gal}}(\nu_0) = T_{\text{Gal}}(\nu_0)$ was fulfilled within the uncertainties, $T_{\text{Gal}}(\nu_0)$ being the measurement we have obtained with TRIS at the frequency $\nu_0 = 600.5$ MHz. We obtained $\beta_{\text{syn}} = 2.95 \pm 0.08$ and $w = 0.13 \pm 0.03$. The results of the fit, together with the data, are shown in Figure 9. This means that in this region of the sky (the Cygnus region) we can assign to the thermal component a weight around 11% of the total emission $[T_{\text{Gal}}(\nu)/T_{\text{Gal}}(\nu_0)]$ at 600 MHz. With this value we obtain an effective spectral index $\beta_{\text{eff}} = 2.84 \pm 0.04$ between 600 and 820 MHz, which is fully consistent with the value found by means of TT-plots, 2.8 ± 0.1. At 1420 MHz we can calculate a weight of the thermal emission around 21% (0.21 ± 0.05), to be compared with the 40% quoted by Reich & Reich (1988a) (in the same way, their value at 408 MHz is between 11% and 16%, while we have found 9% ± 2%). In this case a discrepancy may be ascribed to the fact that we used a very wide beam (~20° FWHM, which intrinsically makes our experiment more sensitive to the more diffuse signals), or it may be simply accidental, since TRIS crossed the Galactic disk in the center direction only in one position. Moreover, we have not considered a possible variation of the synchrotron spectral index between 408 and 600 MHz, but the position of the point at 408 MHz in Figure 9 suggests that $\beta_{\text{syn}}$ flattens at lower frequencies also in the disk region.

4.4. Reconstruction of the 2500 MHz Profile

Having no reliable drift scan at 2500 MHz, we built a profile of the Galactic component starting from the Stockert (Reich & Reich 1986) survey at 1420 MHz. This work is needed in order to extract the CMB signal from the sky temperature.

To obtain the Galactic sky profile at 2500 MHz, we first convolve this map with the beam of the TRIS antennas in order to get the synthetic drift scan at $\delta = +42^\circ$. Then we have to exploit the data available from the analysis described in the previous sections and from Paper II: both (1) the amplitude of the Galactic signal at 600 and 820 MHz and (2) the Galactic spectral index between the

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**Figure 6.** Gray band: Galactic spectral index derived from TT-plots, between the two frequencies that limit each marked interval, in the halo region at $\alpha = 09^h00^m$.

**Figure 7.** Antenna temperature of the Galactic emission (multiplied by a factor $[\nu(\text{MHz})/600]^{2.95}$) at ($\alpha = 09^h00^m$, $\delta = +42^\circ$) (diamonds) and ($\alpha = 10^h00^m$, $\delta = +42^\circ$) (filled circles). The temperature is plotted vs. frequency (MHz). Data points at 150, 408, 820, and 1420 MHz have been obtained after the zero-level adjustment of the maps (see § 4.2).

**Figure 8.** Contour levels of $\nu_0(\text{MHz})$ in the ($E_x$, $B_y$) plane. The two families of lines are referred to $\alpha_1 = 3.0$ (dashed lines) and $\alpha_2 = 2.6$ (solid lines) with $\alpha_1 = 1.7$ (see § 4.3 for explanation). The regions with $400 \leq \nu_0(\text{MHz}) \leq 600$ are shown as distinct (and partially superposed) gray bands for the two cases.

**Figure 9.** Temperature of the Galaxy toward the Cygnus region ($\alpha = 20^h34^m$, $\delta = +42^\circ$). The plot represents $T_{\text{Gal}}(K)/\nu_0^{2.95}$ vs. $\nu$ (MHz), with $\nu_0 = 600.5$ MHz. Diamonds: Experimental points at 408, 600.5, 817.85, 820, and 1420 MHz. The dot-dashed line is the temperature at 600 MHz scaled at the different frequencies with a synchrotron spectral index $\beta_{\text{syn}} = 2.95$. The light gray band represents the result of the two-component (thermal+nonthermal) fit. The error bar at 600.5 MHz is smaller than the plotting symbol. See text for more details.
TRIS frequencies and the 1420 MHz survey in the two sky regions where the TT-plot gives reliable results. Using these quantities, we can extrapolate the pure Galactic contribution from 820 to 1420 MHz knowing the spectral index $\beta_{\text{Gal}}^{\text{TT}}(820, 1420)$. In the regions where this extrapolation is possible, i.e., where $\beta_{\text{Gal}}^{\text{TT}}$ is well defined (that is, in the two regions described in Tables 6 and 7), we can single out a common offset that can be subtracted from the full scan at 1420 MHz. In this way, we obtain a Galactic profile at 1420 MHz, to be further rescaled at 2500 MHz.

Since we need a full sky circle at $\delta = +42^\circ$ at 2500 MHz, in order to rescale the Galactic contribution from 1420 to 2500 MHz, we have to use the spectral index $\beta_{\text{Gal}}^{\text{res}}$ between 600 and 820 MHz, which is well defined everywhere in our right ascension range and, moreover, derived using only measured quantities. In this case, we are assuming that there are no changes in the slope of the Galactic emission at frequencies higher than 820 MHz. This is a safe assumption for the signal coming from the halo (see § 4.3.1), essentially synchrotron emission, while this extrapolation is more critical for regions close to the disk, where the free-free emission is no longer negligible. We could not use the $\beta_{\text{Gal}}^{\text{res}}$ between 820 and 1420 MHz (which a priori would be the natural choice), nor between 600 and 1420 MHz, since its uncertainty does not allow us to recognize the shape of the Galactic profile at 2500 MHz. This is due essentially to the fact that at high Galactic latitudes the Galactic signal at 1420 MHz is of the same order of magnitude as the uncertainty affecting the zero of the temperature scale at this frequency. Following this procedure, we obtain a value of $T_{\text{Gal}} = 91 \pm 93$ mK at $\alpha = 10^\circ 00'$, while the peak value corresponding to the Galactic disk is $471 \pm 93$ mK. Here we quote only the systematic uncertainty that is the dominant one.

The result obtained in this way has been used in Paper II in order to subtract the Galactic contribution from $T_{\text{sky}}$ at 2500 MHz, at Galactic latitudes $b \approx 20^\circ$ (which means one full beam over the Galactic plane).

5. DISCUSSION

5.1. Spectral Coverage, Sky Coverage, and Polarization

If we can choose two frequencies $\nu_1 < \nu_2$ in such a way that in this frequency interval there are no changes in the slope of the radio brightness power law, the spectral index is given in equation (4), provided that we have been able to disentangle the Galactic contribution from the overall signal at the two frequencies. But where we cannot say a priori if there’s a knee in the radio spectrum, using the spectral index derived in this way to estimate the emission at a third frequency $\nu_3$, with $\nu_1 < \nu_3 < \nu_2$, we could be grossly wrong. This is the reason why we could not rely just on the 408 and 1420 MHz surveys to disentangle the Galactic emission, say, from a few absolute data points at 600 and 820 MHz, but rather we needed the reconstruction of sky profiles across the full right ascension range at our frequencies in order to obtain a better characterization of the spectral index. Also a very rough analysis clearly shows that the relative weight of the components of the diffuse radiation is far from being constant. Therefore, the sky coverage should be considered very carefully in a future multi-frequency experiment aimed at the study of the CMB at decimetric wavelengths, since the position difference technique described in Paper II, which proved itself to be particularly effective in component separation, takes advantage exactly from the halo-disk modulation of the Galactic signal.

The TT-plot technique allows us to assign a spectral index to the anisotropic (Galactic) component of the celestial signal regardless of its nature, a step needed in order to separate this contribution from the isotropic ones, that is, the monopole term of the CMB and the integrated effect of unresolved extragalactic radio sources. At 600 and 820 MHz we used our sky profiles without any kind of correction based on external data sets, since for foreground removal, according to the scheme described in Paper II, we needed to single out just the signals as seen by our antennas. A second, straightforward comment, related to polarization issues, is that in principle the spectral index given in Table 1, even if looking at the Galactic halo where synchrotron is the dominant mechanism, is not rigorously the true synchrotron spectral index, which instead is intimately linked to the degree of polarization of the radiation. Nevertheless, (1) this was what we needed for TRIS immediate purposes, and (2) we checked that the correction for polarization produces an effect comparable to the uncertainty affecting the determination of $\beta_{\text{Gal}}$ itself, probably due to beam depolarization. Therefore, in view of future experimental programs, we stress that a dual-polarization system, although not mandatory, would allow (1) a better control of systematic effects, (2) the direct measurement of the full (polarized+unpolarized) sky temperature, and, as an ancillary result, (3) it could produce an important advance in the knowledge of the diffuse Galactic radio emission.

5.2. The Effect of Base-Level Corrections on the Local Spectral Index

We conclude this section with some further remarks concerning our analysis of the zero levels of continuum surveys used in this work. We emphasize that, at least in the northern sky, where direct measurements have been carried out, the choice of the new zero levels we suggest in § 4.2 should be done in order to prevent base-level effects in the determination of the local Galactic spectral index. We checked the effect of this correction on the local spectral index calculated using the sky profiles at 408 and 1420 MHz extracted from the destriped maps (Platania et al. 2003). The effect is obviously a general steepening in the spectrum, since a higher temperature is associated with the 408 MHz profile, but while this effect is practically negligible around the Cygnus region (Galactic disk), since its value here is $\Delta \beta \approx +0.04$, it is decisive around the minimum of the Galactic signal at $\delta = +42^\circ$ (Galactic halo), where $\Delta \beta \approx +0.2$. Generally speaking, the steepening will be more pronounced at high Galactic latitudes, where the Galactic emission becomes fainter and fainter and where the signal is comparable with the constant base-level correction. A further investigation of this effect is not in the purposes of this paper, but nevertheless we suggest that it should be carried out in future works. We recall that the problem of the flattening of the radio spectrum between 408 and 1420 MHz at high Galactic latitudes, even at an angular resolution of 2', has already been noticed and discussed by Reich & Reich (1988a) on the basis of their spectral index map (whose absolute spectral index error is $\pm 0.1$; Reich & Reich 1988b), within the framework of a Galactic wind model. Some years later, and from a different viewpoint, this problem has been noted by Davies et al. (1996) studying a strip of sky centered at $\delta = +40^\circ$. In fact, using TT-plots, they have found a steepening of the spectral index going from the Galactic plane toward the halo, and, in the same work, they suggested also the existence of a base-level residual $\sim 3.5$ K in the 408 MHz survey ($\sim 0.15$ K at 1420 MHz). The correction of the zero levels of these maps we have suggested in Table 9 seems to solve the problems, but we think that a further analysis based on a better removal of base-level effects and new observations are essential to clarify the situation.

6. CONCLUSIONS

The main purpose of the study we presented in this paper was to evaluate the Galactic diffuse emission at decimetric wavelengths at $\delta = +42^\circ$. This work is necessary to extract the temperature of
the CMB at frequencies close to 1 GHz from TRIS absolute measurements. In fact, distortions of the blackbody CMB spectrum are expected at decimetric wavelengths (Paper II).

We extended, however, our analysis of the Galactic signals and added to our measurements data in literature covering the frequency range 150–1420 MHz. We conclude that at angular resolutions of $\sim 20^\circ$ (1) the steepening of the Galactic spectral index from $\beta_{\text{Gal}} \approx 2.3$–2.5 to $\beta_{\text{Gal}} \approx 2.8$–3.0 at high Galactic latitude is confirmed; (2) the change of slope is maximum between 408 and 600 MHz; (3) this behavior is fully compatible with the features of the CRE energy spectrum and the intensity of the Galactic magnetic field; (4) in the disk the signal is a mixture of synchrotron and thermal emission from H ii regions, with H ii contribution to $T_{\text{Gal}}$ variable from 11% at 600 MHz to 21% at 1420 MHz; and (5) the polarization of the synchrotron radiation affects less than 1% of the spectral index values.

We have also shown, in § 3.3, how a detailed knowledge of the spectral index can help in recognizing and eventually controlling systematic uncertainties affecting absolute temperature scans. The impact of the polarization on the knowledge of the Galactic spectral index has been evaluated, and, for an experiment like TRIS, with a beam around $\sim 20^\circ$ FWHM, we have shown that it is negligible everywhere, especially toward the Galactic disk, even if there may be a suggestion that depolarization is less effective in the sky region $5^\circ \leq \alpha \leq 8^\circ$ (at $\delta = +42^\circ$), going from the anticenter toward the halo in the northern direction (see Fig. 5).

TRIS 600 MHz data are accurate enough to allow a critical discussion of the zero level of the surveys at 150, 408, 820, and 1420 MHz, at least in the northern sky where our observations have been done. The results, obtained as described in § 4.2 and discussed at the end of the previous section, are summarized in Table 9. The effect of this new assessment of the zero levels on the evaluation of the spectral index between 408 and 1420 MHz is also considered: a substantial steepening of the local spectral index, with $\Delta \beta \approx +0.2$, is observed toward the regions at high Galactic latitude, at TRIS angular resolution. This adjustment is important because these maps, noticeably the 408 MHz map (Haslam et al. 1982), are frequently used as a benchmark in astrophysical and cosmological studies, e.g., for searching CMB anisotropies (e.g., Planck mission, Tauber 2004; SPOT mission, Cortiglioni et al. 2004) and in planning future observation of the diffuse radiation from space or from ground stations.

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REFERENCES

Hoaglin, D. C., Mosteller, F., & Tukey, J. W. 1983, Understanding Robust and Exploratory Data Analysis (New York: Wiley)
Nishimura, J., et al. 1990, in Proc. 21st Int. Cosmic Ray Conf. (Adelaide), 213
Reich, P., & Reich, W. 1986, A&AS, 63, 205
Sironi, G. 1969, Planet. Space Sci., 17, 11